

Sampling

Component Knowledge

- Know the difference between random sampling and stratified sampling
- To know how to take a random sample
- To know how to calculate sample sizes for stratified sampling

		<u>Key Voc</u>	abular	ч		
Qualitative data	Data co ethnicit	llected that is descr y.	ibed in	words not	numbers.	e.g. race, hair colour,
Quantitative data	This is the collection of numerical data that is either discrete or continuous.					
Population	This is t	he whole group you	i are co	llecting dat	a from.	
Sample	A samp	e is part of the who	le popu	ulation.		
Simple Ra	ndom Sar	npling			<u>Syste</u>	ematic sampling
A simple random sample is when each memb under study has the same chance or probabi for the sample.		ember of the populat pability of being selec	ion ted	 This is a very similar method to random sampling, but the population would first be ordered according to specific criteria such a 		ilar method to random population would first be to specific criteria such as
An example of a simple randor	n sample w	ould be:		listing nar	nes of pe	ople in the population in
1. Assign a number to every m	nember of t	he population		aiphabeth	cal oluel.	
2. Randomly generate numbers using numbers from a hat or a computer calculator			 The sample would be drawn by selecting every nth person. For example, every 10th person in the list. 			
3. Use the data from the corre	sponding m	embers of the				
population				<u>Onlin</u>	e clip	A sample should be:
The following options are not a same chance of being chosen:	random as r	not everyone has the		U1	62	 fair and unbiased
• Choose the first 50 people who arrive at the office.						 large enough in size
• Choose 50 people whose sur	name begir	ns with J or T.		 		to be representative of the whole population
• List all the office workers in alphabetical order and choose every 5th name on the list.			ery			under study.
		Stratified	Samplir	ng		
A stratified sample involves sample from each class (e.g	grouping . grouped	members of the pop by age, language et	oulatior c.)	n into classe	es before	taking a proportionate
To find the amount of people in each class we must do the following calculation $\frac{Class size}{total nonvertices} \times sample size$						
<u>Example</u>					Г	population
The table below shows the age group of the members of a tennis			s club.		Total population=	
	Ag	e Group Junior	Adult	Senio	r	320 + 500+ 130 = 950
	Nu	umber 320	500	130		
A stratified sample of 40 is t	A stratified sample of 40 is to be taken. Calculate the number for each age group in the sample.					
Junior		Adı	ult			Senior
$\frac{320}{950} \times 40 = 13.5 \approx 14 pe$	4 people $\frac{500}{950} \times 40 = 21.1 \approx 21 people$ $\frac{130}{950} \times 40 = 5.4 \approx 5 people$			$40 = 5.4 \approx 5 \ people$		

Averages from a



frequency table

Component Knowledge

• To be able to calculate the mean, median, mode and range from a frequency table.

	<u>K</u>	ey vocabulary				
Frequency	The number of pi	The number of pieces of data we have.				
Mean	Add up the value	Add up the values you are given and divide by the number of values you				
	have.	have.				
Median	The middle value	when the data is	in order.			
Mode	The value or item	n with the highest	trequent	Cy.		
Range	This is the difference between the largest and smallest values. Shows the spread of the data					
A team played 10 gar	nes and recorded the nu	mber of goals sco	ored in the	ose games.		
Goal scored (x)	Frequency (f)	Total Frequ far	uency so $(fx)(f multiplied by$			
0	2	(2)	2	0 x 2 = 0		
1	2	(2+2)	4	1 x 2 = 2		
2	5	(2+2+5)	9	2 x 5 = 10		
3	1	(2+2+5+1)	10	3 x 1 = 3		
Total	10			15		
Step 3: calculate the mean using the formula $\frac{total fx}{total frequency}$ Mean = $\frac{15}{10}$ = $\frac{1.5 \text{ goals}}{10}$			Highes scored <u>Mode</u>	t frequency = 5 for 2 goals = 2 goals scored		
Calculating the mean $\frac{To}{To}$	dian number of goals sc atal frequency+1 2	<u>ored.</u>	<u>Calcula</u> goals s	ating the range number of cored.		
$\frac{11}{1}$ = 5.5 th value			Highes	t number of goals = 3		
2 - 3.3 Value	add the frequency co	lumn until	Lowest number of goals = 0			
	you reach the value i the 5 th and 6 th value	n-between	Range = 3 – 0			
iviedian = 2 goals				<u>Range = 3</u>		



Probability



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Component Knowledge

• Understand what probability shows

- Understand probability notation
- Write a probability of a single event

	<u>Key Vocabulary</u>
Probability	The mathematical chance, likelihood, of an outcome happening
Event	The "thing" that is being completed/done/observed/counted
(Event) Outcome	What happens when the event is performed
Probability scale	A numerical scale from 0 to 1, with 0 being an impossible outcome and 1 being an outcome certain to happen
Mutually exclusive (event) outcomes	When outcomes cannot happen at the same time eg being an adult and being a child, you cannot be both
Exhaustive (event) outcomes	When a set of outcome cover all possibility with no gaps eg it snowing and it not raining
Probability: The probability of	of an (event) outcome A, happening is number of ways outcome A can happen
P (Outo	$\frac{\partial d}{\partial d} = \frac{\partial d}{\partial d} \frac{\partial d}{\partial d} \frac{\partial d}{\partial d} $
e.g. the probabili	ity of rolling a number 4 on a regular 6 sided dice
Outcome "4": 4 , s	o 1 option $P(roll a 4) = \frac{1}{6}$
All possible outco	omes: 1 , 2 , 3 , 4 , 5 or 6, so 6 possibilities altogther
e.g. the probabili dice	ity of rolling a number greater than 4 on a regular 6 sided
Outcomes "greate	er than 4": 5 or 6 , so 2 options
	$P(roll\ a\ number\ greater\ than\ 4) = \frac{2}{6}$
All possible outco	omes: 1 , 2 , 3 , 4 , 5 or 6, so 6 possibilities altogther
	<u>Online clips</u>
	M655, M941, M938, M755

<u>Tree diagrams</u>

independent

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Component Knowledge

- Fill in missing values on a tree diagram
- Complete a tree diagram
- Find probabilities from a tree diagram

<u>Key Vocabulary</u>

Independent	An event that is not affected by other events		
Probability	The chance that something happens		
Event	One (or more) outcomes of an experiment		
Outcome	A possible result of an experiment		
Tree diagram	A diagram of lines connecting nodes, with paths that go outwards and do not loop back		

Key Concepts

Independent events are events which do not affect one another.

Eg – replacing a counter before taking another from a bag

Probabilities on each set on branches add up to 1.

Probabilities can be written as fractions or decimals.

Probability Rules

The AND rule for probability states that the probability of A and B is the probability of A x the probability of B

The OR rule for probability states that the probability of A or B is the probability of A + the probability of B

Example

There are red and blue counters in a bag.

The probability that a red counter is chosen is 2/9.

A counter is chosen and replaced, then a second counter is chosen.

Draw a tree diagram and calculate the probability that two counters of the same colour are chosen.



Prob of two reds: $\frac{2}{9} \times \frac{2}{9} = \frac{4}{81}$ Prob of two blues : $\frac{7}{9} \times \frac{7}{9} = \frac{49}{81}$ Prob of same colours: $4 \quad 49 \quad 53$

 $\frac{4}{81} + \frac{49}{81} = \frac{53}{81}$

Note – the probability of a blue counter is found by doing 1 - 2/9 to give 7/9

Online clips

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Tree dia<u>grams -</u>



dependent

Component Knowledge

- Draw a probability tree for dependent events
- Calculate probabilities from a dependent event tree diagram

Key Vocabulary Probability The chance that something will happen Event The outcome of a probability Tree diagrams show all the possible outcomes of an event and helps to calculate their Tree diagram probabilities. Each set of branches must add up to 1. The outcome of a previous event does influence/affect the outcome of a second event. Dependent Outcome The result of a single performance of an experiment AND rule The outcome has to satisfy both conditions at the same time. Multiply the probabilities together. The outcome has to satisfy one condition, or the other, or both. Add the probabilities OR rule together. **Dependent tree diagrams** There are black and white marbles in the box. One is picked – and not replaced – then another is picked. Draw a probability tree to show this information. 2nd Pick 1st Pick 2 Black 8 3 Black 9 6 White 8 Black 8 White 9 5 White 8 Subtract 1 away from the numerator on these two because one of the Subtract 1 away from marbles of this colour the denominator on has been removed

these sets of branches as one marble has been

removed







Example: 80 children went on a school trip.

They went to London or to York.

23 boys and 19 girls went to London.

14 boys went to York.

(a) Use this information to complete the two-way table.

Step 2- calculate missing values using the known values. Remember both the horizontal and vertical totals must equal the overall total, in the case below, = 80.


Interpreting two-way tables

We can now use the fully completed two-way table to interpret the data.

	London	York	Total
Boys	23	14	37
Girls	19	24	43
Total	42	38	80

Questions could look like this:

a) How many students went to London?

We can read from the table vertically and see there were 42 students who visited

b) One of these 80 students is chosen at random.What is the probability that this student visited London?

We can read from the table vertically and see there were 42 students who visited London.

So, the $P(a \text{ student visits London}) = \frac{42}{80}$

c) A student is picked at random.

Given they are a girl, what is the probability they went to York?

We can read the table to find the total girls = 43 and the girls who visited York = 24

So, the *P*(given the student is a girl, they visit York) = $\frac{24}{42}$

<u>Online clip</u>

M899



Error In	torvola	Component Knowledge		
Error in	tervais :	component knowledge		
		 To use understand how to round to different 		
		degrees of accuracy.		
VV ¥		• To be able to write error intervals when rounding		
		using correct inequality notation.		
		• To be able to write error intervals when rounding		
		using correct inequality notation.		
	<u>Key Vo</u>	ocabulary		
Rounding	Rounding means making	a number simpler but keeping its value close to what it		
	was. The result is less acc	urate, but easier to use.		
Accuracy	How close the rounded va	alue is to the original value.		
Place value	The value of the digit in a	number		
Lower bound	The smallest possible value	ue that can be rounded to the number given.		
Upper bound	The largest possible value	e the rounded value can take.		
Truncation	Truncation comes from th	ne word truncare, meaning "to shorten". The number is		
	cut off at a certain point.			
	equal to one another.			
Inequality Notat	ION All error intervals look th	ne same like this:		
	<	n <		
The value, n, can	be greater or equal to	The value, n, can only be less than this number but		
this number.		we use it to make any calculations easier to		
		perform, should we need to.		
Ennon intonvola "				
<u>error intervais-r</u>	ounding according to pi	lace value		
Example 1- Frank rounds nearest ten. His result is interval for y.	a number, y, to the 50 Write down the error	Example 2- Freya rounds a number, n, to one decimal place. Her result is 6.4 Write down the error interval for n.		
Begin by finding the ten, i	n this case, greater than	Begin by finding the tenth, in this case, greater than		
and less than 50.		and less than 6.4. (Note: 1dp = tenths column.)		
Bange of w	alues y can take			
Range of V	aldes y call take	Range of values n can take		
45	55	6.45		
40	50 80	6.3 6.4 6.5		
The midpoint between 40 and 50 is 45. This is the lower bound.		The midpoint between 6.3 and 6.4 is 6.35. This is the lower bound.		
The midpoint between	50 and 60 is 55. This the	The midpoint between 6.4 and 6.5 is 6.45. This		
upper bound (this can never = 55 but can be as		the upper bound (this can never = 6.45 but can		
large as 54 000000	55 is easier to calculate	$b_{\text{p}} = b_{\text{p}} $		
with Additionally way		NC as laige as 0.4777777777 0.47 is easier 10		
with. Additionally, we use < as well.				
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	ise < as well.	calculate with. Additionally, we use < as well.		

The answer is $6.35 \le n < 6.45$.

The answer is $45 \le y < 55$.

Error intervals - rounding according to significant figures

Depending on the size of the number, the rounding will change when rounding to significant figures. Rounding like this keeps all numbers rounded to the same degree of accuracy relative to the size of the number.

Example 3- A number, g, is 15,000 when rounded to 2 significant figures. Write down the error interval.

Begin by finding the place value of the 2nd significant figure, in this case, this is 5000. This means we are rounding to 2 sig figs = rounding to nearest thousand.



The midpoint between 14,000 and 15,000 is 14500. This is the lower bound.

The midpoint between 15,000 and 16,000 is 15,500. This the upper bound.

The answer is $14,500 \le g < 15,500$.

Error intervals - truncation

Example 4- A number, x, is 0.07 when rounded to 1 significant figure. Write down the error interval.

Begin by finding the place value of the 1st significant figure, in this case, this is 0.07. This means we are rounding to 1 sig fig =rounding to nearest hundredth.



The midpoint between 0.06 and 0.07 is 0.065. This is the lower bound.

The midpoint between 0.07 and 0.08 is 0.075. This the upper bound.

The answer is $0.065 \le x < 0.075$.

Be careful when reading error interval questions as truncating is not rounding like place value. The number has been "chopped", which means the value given **IS THE LOWER BOUND.** It commonly applies to decimals.

Example 5- State the error interval of 4.5 when it has been truncated to 1 decimal place.

Begin by finding the tenth, in this case, greater than 4.5. (**Note: 1dp = tenths column.)** This is the upper bound.

Remember: the value cannot equal 4.6!



The answer is $4.5 \le n < 4.6$.



M730

Inequalit Wis	ties • Ur • Re nu • De • Fo	<u>Component Knowledge</u> nderstand and use inequality notation present the solution set of an inequality on a mber line ecide whether a number satisfies an inequality rm an inequality from a question and solve it	
Inequality Less than Less than or equal to Greater than Greater than or equal to Integer	<u>Key Vocat</u> An inequality shows that two This is shown by the symbol This is shown by the symbol This is shown by the symbol This is shown by the symbol A whole number	<pre>pulary o quantities are (may) not be equal < < < < < > > > > > </pre>	
Notation $x > 2$ means x is greater than 2 $x < 3$ means x is less than 3 $x \ge 1$ means x is greater than or equal to 1 $x \le 6$ means x is less than or equal to 6		Examples: $x \ge 1$ is true for $x = 6, 2.5$ and 1 $x < 5$ is false for $x = 10, 5.05$ and 5The set of <i>integers</i> which satisfy $-2 \le x < 3$ is $\{-2, -1, 0, 1, 2\}$	
The set of number x is less than 4 x < 4 + is less than or equal to + is less than or equal to + is greater + is greater	rs satisfying an inequality 4 4 5 4 5 5 5 5 5 5 5 5	can be represented on a number line: $2 < x < 10$ $-2 \le x \le 5$ $-2 \le x \le 5$ $-2 \le x \le 5$ $-2 \le x \le 11$ $-2 \le x \le 11$ $-7 \le x < 15$	

